

# Designing Agile Banking Supervision

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- Banking supervision faces three key challenges.
  - ① there is incomplete information about various risks within the economy spread across the supervisor and the banks
    - banks have very detailed views of their own portfolios, but they cannot look into the business lines of their peers
    - supervisor, on the other hand, is able to probe into portfolios across all of his supervised institutions, despite a lack of finer details
  - ② there is a conflict of interest between the banks and the supervisor
    - banks tend to have greater risk appetite than the supervisor
- To achieve socially desirable outcome, supervisory authorities design their public messages to guide and monitor bank behaviors.
  - while the cost of supervisory objection is rigid given the legal setup, supervisory communication should be an agile response to the fluid informational dynamics.

# This Paper

- We model banking supervision as a game of strategic communication, and solve for the supervisor's optimal communication strategy.
  - incomplete information about the state of the economy
    - each of the bank and the supervisor receives a private signal
  - a conflict of interest between the banks and the supervisor
    - the bank prefers high risk endeavors to conservative risk taking in every state of the economy
    - the supervisor prefers high risk endeavors only if the state of the economy is good
  - before the bank takes its action, the supervisor recommends how to act
    - "be aggressive regardless of your signal"
    - "be aggressive only if your signal is good"
    - "be conservative regardless of your signal"
  - after the bank takes its action, the supervisor can object to the action
    - costly change from aggressive risk level to conservative risk level

- We find that an increase in the bank's informational advantage ( $\gamma$ ) has two distinct effects.
  - ① the information effect (dominates when  $\gamma$  is small)
    - an increase in  $\gamma$  enables the supervisor to make more informed supervisory decisions when he can induce the bank to reveal its information and, therefore, improves welfare
  - ② control dilution (dominates when  $\gamma$  is large)
    - an increase in  $\gamma$  reduces the probability that the bank thinks the supervisor will object to its aggressive risk-taking
    - this implies that the bank reveals information less frequently and, therefore, welfare deteriorates
- The welfare effect of increased private information in the hands of the private sector is non-monotonic!
- The bank's cost in case of supervisory objection ought to be set high.
  - intuitively, what the bank cares about is the “cost-adjusted” probability that the supervisor will object to its aggressive risk-taking

# The Model

- There is a bank and a supervisor.
- The bank decides whether to take high risks (“Aggressive”) or take low risks (“Conservative”).
  - The payoff from high risk endeavors is  $u_\omega$  for the bank and  $v_\omega$  for the supervisor.
    - $\omega \in \{G, B\}$  is the state of the economy
  - The payoff from conservative risk taking is normalized to zero for both the bank and the supervisor.
    - all that matters is the *relative gains* from taking on high risk endeavors
  - We focus on the case where there is a conflict of interest between the bank and the supervisor:

$$u_G = u_B > 0 \text{ and } v_G > 0 > v_B.$$

- 1 the bank prefers high risk endeavors to conservative risk taking in every state of the economy
- 2 the supervisor prefers high risk endeavors only if the state of the economy is good

- In this case, the payoff from aggressive risk-taking when  $\omega = G$  can be further normalized to one for both the bank and the supervisor:

$$u_G = v_G = 1.$$

- Given our assumptions on payoffs,  $u_B = 1$  and

$$v_B = -d, \quad d > 0.$$

# The Model: Incomplete Information

- Both the bank and the supervisor do not observe  $\omega$ , but each of them receives a private signal about the state of the economy.
  - the bank's signal  $s$  takes one of two values,  $g$  or  $b$ :

$$\gamma = \Pr(s = g | \omega = G) = \Pr(s = b | \omega = B)$$

- $\gamma \in (\frac{1}{2}, 1)$  implies that the signal is indeed informative about the state and the bank does not perfectly observe  $\omega$
- the supervisor observes the probability  $t$  that  $\omega = G$ :

$$t \sim F_{[0,1]}$$

- $t$  is the supervisor's "type"
  - this formulation is equivalent to the standard one in which we would specify the prior probability  $t_0$  that  $\omega = G$  and the supervisor's signal  $s' \in [\underline{s}, \bar{s}]$  that has CDF  $F_\omega$  conditional on  $\omega$

# The Model: After the Bank Decides on Its Risk Level

- The supervisor assesses the bank's risk-management practices.
  - ① he observes its risk level
  - ② decides whether to allow or object to its risk-management practices
- If the supervisor allows the bank's risk-management practices, it keeps its risk level intact as it chose.
- If the supervisor objects to the bank's risk-management practices, it is forced to readjust its risk level to be low.
  - in this case, the bank incurs a cost  $c > 0$ 
    - $c$  can represent the fact that the bank may be forced to sell its high-risk assets at fire sale prices
    - $c$  can reflect the bank's cost of reputation loss
- An implicit assumption here is that the supervisor *never* objects to a conservative bank.



# The Model: Before the Bank Decides on Its Risk Level

- The supervisor discloses information about his type  $t$ .
- The supervisor's communication strategy is modeled following the recent literature on information design.
  - 1 an arbitrary finite set  $M$  of messages
  - 2 a function  $\pi : [0, 1] \rightarrow M$ 
    - $\pi(t)$  denotes the message that the supervisor of type  $t$  picks to send
- We let  $F(\cdot | m)$  represent the bank's posterior belief distribution about the supervisor's type  $t$  after observing  $m \in M$
- We let  $\delta(m) \in \{0, 1\}$  denote the bank's (observed) risk level following message  $m \in M$ 
  - 1 stands for "Aggressive"
  - 0 stands for "Conservative"

# The Model: The Timing of the Game

- 1 The supervisor publicly commits to his communication strategy  $(M, \pi)$ .
- 2 Nature chooses  $\omega$ , the bank observes  $s$ , and the regulator observes  $t$ .
- 3 The supervisor discloses information about  $t$  according to his communication strategy.
- 4 The bank decides whether to take high risks (“Aggressive”) or take low risks (“Conservative”).
- 5 The supervisor assesses the bank’s risk-management practices.
  - if the bank is aggressive, he decides whether to accept or object to its risk-management practices
- 6 Finally, the payoffs are realized.

# Preliminaries: Supervisor's Policy

- Let  $q$  denote the probability that the supervisor thinks the state of the economy is good ( $\omega = G$ ).
  - If the bank is aggressive, the supervisor's expected payoff is

$$qv_G + (1 - q)v_B = q - (1 - q)d.$$

- If the bank is conservative, the supervisor's payoff is zero.
- Hence, he allows the bank's aggressive risk-taking if and only if

$$q \geq \hat{t} := \frac{d}{1 + d}.$$

- based solely on his private information, the supervisor allows aggressive risk-taking if and only if  $t \geq \hat{t}$

# Preliminaries: Supervisor's Policy, Cont.

- In equilibrium, the bank can be
  - aggressive regardless of its signal
    - in this case, the supervisor will allow the bank to be aggressive iff  $t \geq \hat{t}$
  - aggressive if its signal was good and conservative if its signal was bad
    - in this case, the supervisor will learn that  $s = g$  ( $s = b$ ) from observing that the bank is aggressive (conservative)
    - based on his type &  $s = g$ , the supervisor will allow the bank to be aggressive iff

$$\Pr(\omega = G | s = g, t) = \frac{\gamma t}{\gamma t + (1 - \gamma)(1 - t)} \geq \hat{t}$$
$$t \geq \underline{t} = \frac{(1 - \gamma)d}{\gamma + (1 - \gamma)d} (< \hat{t})$$

- conservative regardless of its signal

# Supervisor's Problem

$$\max_{T^{(1,0)}, T^{(1,1)} \subset [0,1]} \int_{T^{(1,0)} \cap [\underline{t}, 1]} [\gamma t - (1 - \gamma)(1 - t) d] dF(t) + \int_{T^{(1,1)} \cap [\hat{t}, 1]} [t - (1 - t) d] dF(t)$$

- $t \in T^{(1,0)}$ : guide the bank to be aggressive only if its signal is good
  - BUT object to aggressive risk-taking if  $t \in T^{(1,0)} \cap [0, \underline{t})$ 
    - this *does* happen in equilibrium
- $t \in T^{(1,1)}$ : guide the bank to be aggressive regardless of its signal
  - BUT object to aggressive risk-taking if  $t \in T^{(1,1)} \cap [0, \hat{t})$ 
    - this will *not* happen in equilibrium
- $t \in T^{(0,0)} := [0, 1] \setminus (T^{(1,0)} \cup T^{(1,1)})$ : guide the bank to be conservative regardless of its signal

# Supervisor's Problem, Cont.

subject to a set of incentive compatibility constraints for the bank:

$$\Pr(t \geq \underline{t} | s = g, m = (1, 0)) \geq c / (1 + c) \quad (IC_g^{(1,0)})$$

$$\Pr(t \geq \underline{t} | s = b, m = (1, 0)) \leq c / (1 + c) \quad (IC_b^{(1,0)})$$

$$\Pr(t \geq \hat{t} | s = g, m = (1, 1)) \geq c / (1 + c) \quad (IC_g^{(1,1)})$$

$$\Pr(t \geq \hat{t} | s = b, m = (1, 1)) \geq c / (1 + c) \quad (IC_b^{(1,1)})$$

$$\Pr(t \geq \hat{t} | s = g, m = (0, 0)) \leq c / (1 + c) \quad (IC_g^{(0,0)})$$

$$\Pr(t \geq \hat{t} | s = b, m = (0, 0)) \leq c / (1 + c) \quad (IC_b^{(0,0)})$$

$$\begin{aligned} \Pr(t \geq \underline{t} | s = b, m = (1, 0)) &= \frac{\int_{T^{(1,0)} \cap [\underline{t}, 1]} [(1 - \gamma)t + \gamma(1 - t)] dF(t)}{\int_{T^{(1,0)}} [(1 - \gamma)t + \gamma(1 - t)] dF(t)} \\ &\leq \hat{p} = \frac{c}{1 + c} \end{aligned}$$

# Solution to the Supervisor's Problem

- $t \in \mathcal{T}^{(1,0)} = [0, \tau) \cup [\tau_*(\lambda^*), \tau^*(\lambda^*))$ , where  $\tau \leq \underline{t}$  and  $[\tau_*(\lambda^*), \tau^*(\lambda^*)) \subset [\underline{t}, \bar{t}]$ : guide the bank to be aggressive only if its signal is good
  - BUT object to aggressive risk-taking if  $t \in [0, \tau)$ 
    - the bank thinks  $t \in [0, \tau)$  if it has  $s = g$  and receives the message  $(1, 0)$
    - the bank thinks  $t \in [\tau_*(\lambda^*), \tau^*(\lambda^*))$  if it has  $s = b$  and receives the message  $(1, 0)$
  - $[\tau_*(\lambda^*), \tau^*(\lambda^*)) \nearrow [\underline{t}, \bar{t}]$  as  $\lambda^* \searrow 0$  and  $[\tau_*(\lambda^*), \tau^*(\lambda^*)) \searrow \hat{t}$  as  $\lambda^* \nearrow \bar{\lambda}$
- $t \in \mathcal{T}^{(1,1)} = [\tau^*(\lambda^*), 1]$ : guide the bank to be aggressive regardless of its signal
  - AND *do* allow aggressive risk-taking
- $t \in \mathcal{T}^{(0,0)} = [\tau, \tau_*(\lambda^*))$ : guide the bank to be conservative regardless of its signal

## Solution to the Supervisor's Problem, Cont.

- If the IC constraint is *not* binding,  $\lambda^* = 0$ ,  $\tau_* = \underline{t}$ ,  $\tau^* = \bar{t}$  and solve

$$\int_{\underline{t}}^{\bar{t}} [(1 - \gamma)t + \gamma(1 - t)] dF(t) = c \int_0^{\tau} [(1 - \gamma)t + \gamma(1 - t)] dF(t)$$

for  $\tau$ .

- If the IC constraint is binding,  $\tau = \underline{t}$  and solve

$$\int_{\tau_*(\lambda^*)}^{\tau^*(\lambda^*)} [(1 - \gamma)t + \gamma(1 - t)] dF(t) = c \int_0^{\underline{t}} [(1 - \gamma)t + \gamma(1 - t)] dF(t) \quad (1)$$

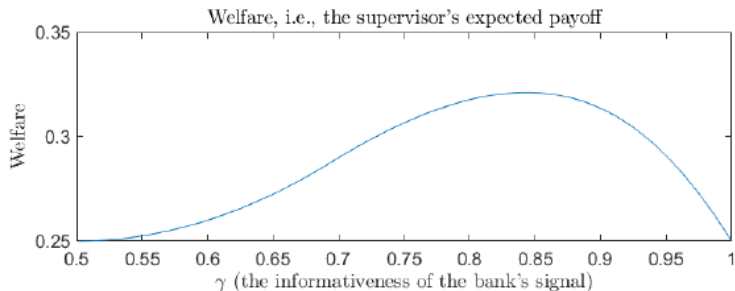
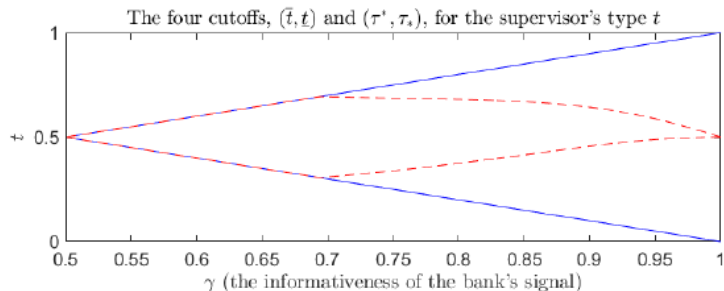
for  $\lambda^*$ , which in turn implies  $\tau^*$  and  $\tau_*$ .

### Proposition

*If  $\gamma$  is sufficiently close to  $\frac{1}{2}$ , then the supervisor's expected payoff increases in  $\gamma$ . For  $\gamma$  sufficiently close to 1, the supervisor's expected payoff decreases in  $\gamma$ .*



# An Example



# An Example, Cont.

- $\bar{t}$  is upward-sloping, while  $\underline{t}$  is downward-sloping
  - an increase in  $\gamma$  expanding the *ideal* information-acquisition region  $[\underline{t}, \bar{t}]$ .
- $\tau^*$  is initially  $\nearrow$  but eventually  $\searrow$ ,  $\tau_*$  is initially  $\searrow$  but eventually  $\nearrow$ 
  - an increase in  $\gamma$  is initially expanding but eventually shrinking the *actual* information-acquisition region  $[\tau_*, \tau^*]$ .
  - As  $\gamma$  increases, notice that the default-objection region  $[0, \underline{t})$  contracts, which makes it more challenging to satisfy the incentive constraint (1).
    - This forces the supervisor to eventually shrinking the actual IA region despite the ever expanding ideal IA region.

## • Welfare

- 1  $\uparrow$  in  $\gamma$  initially expands (eventually shrinks) the actual IA region  $[\tau_*, \tau^*]$ 
  - the bank reveals information more (less) frequently
  - therefore, welfare improves (deteriorates).
- 2  $\uparrow$  in  $\gamma$  has another effect of enabling the supervisor to make more informed decisions within the actual IA region
  - therefore, welfare continues to improve beyond the point at which  $[\tau_*, \tau^*)$  starts to shrink

$$\int_{\tau_*(\lambda^*)}^{\tau^*(\lambda^*)} [\gamma - (2\gamma - 1) t] dF(t) = c \int_0^{\underline{t}} [\gamma - (2\gamma - 1) t] dF(t)$$
$$\Pr(t \geq \underline{t}, s = b, m = (1, 0)) = c \Pr(t < \underline{t}, s = b, m = (1, 0))$$

- We find that an increase in the bank's informational advantage ( $\gamma$ ) has two distinct effects.
  - 1 the information effect (dominates when  $\gamma$  is small)
    - an increase in  $\gamma$  enables the supervisor to make more informed supervisory decisions when he can induce the bank to reveal its information and, therefore, improves welfare
  - 2 control dilution (dominates when  $\gamma$  is large)
    - an increase in  $\gamma$  reduces the probability that the bank thinks the supervisor will object to its aggressive risk-taking
    - this implies that the bank reveals information less frequently and, therefore, welfare deteriorates

# Comparison to the Cheap-Talk Equilibrium

## Proposition

*There always exists a cheap-talk equilibrium in which the supervisor sends the message  $m = (1, 1)$  if he is of type  $t \geq \hat{t}$  and  $m = (0, 0)$  otherwise; the bank is aggressive if and only if it receives message  $m = (1, 1)$ , in which case the supervisor will allow it to be aggressive.*

- Notice that in the limit as  $\gamma \rightarrow \frac{1}{2}$  or  $\gamma \rightarrow 1$ , the supervisor's expected payoff shrinks to his expected payoff in the cheap-talk equilibrium presented in the above proposition.
  - in the former case, the supervisor chooses not to induce the bank to act on its own information
  - in the latter case, he cannot induce the bank to act on its own information
- Compared to this cheap-talk equilibrium, commitment power on the supervisor's side improves welfare as long as the bank has some but not perfect information about the state.

## Proposition

*Suppose that the IC constraint is not binding. Then the supervisor's unconstrained optimum is a cheap-talk equilibrium: the supervisor sends the message  $m = (1, 1)$  if he is of type  $t \geq \bar{t}$ ,  $m = (1, 0)$  if he is of type  $t \in [0, \tau) \cup [\underline{t}, \bar{t})$  for some  $\tau \in [0, \underline{t}]$ , and  $m = (0, 0)$  otherwise.*

- In light of this proposition, we conclude that a sufficient condition for the supervisor's commitment power to improve welfare is that  $\gamma \in (\gamma_*, 1)$ , where  $\gamma_* \in (\frac{1}{2}, 1)$  such that  $\gamma > \gamma_*$  implies the IC constraint is binding:
  - 1  $\gamma > \gamma_*$  ensures that the supervisor is actually using the commitment power vested in him
  - 2  $\gamma < 1$  ensures that the supervisor has plausible deniability he will not always allow aggressive risk-taking even if he is of type  $t \in [\underline{t}, \bar{t})$
- Note that welfare improvements from commitment power is still non-monotonic in  $\gamma$ .

# Bank's Cost in Case of Supervisory Objection

- One crucial lesson from our analysis is that whether the IC constraint for the bank is binding or not plays a key role in determining the welfare implications of more information on the bank's side.
- Looking at

$$\int_{T_{\text{Allow}}^{(1,0)}} [(1-\gamma)t + \gamma(1-t)] dF(t) \leq c \int_0^t [(1-\gamma)t + \gamma(1-t)] dF(t), \quad (2)$$

it is immediate that increasing  $c$  relaxes it, ergo improving welfare until the IC constraint is no longer binding.

## Proposition

*Let  $v(c)$  denote the supervisor's maximal attainable payoff when the bank is faced with a cost  $c$  in case of supervisory objection. Then  $v(c)$  is strictly increasing for  $c \in [0, c^*)$  and is equal to  $v(c^*)$  for  $c \geq c^*$ , where  $c^* > 0$  is the value of  $c$  such that (2) holds with equality.*

# Bank's Cost in Case of Supervisory Objection, Cont.

- Intuitively, the bank is worried about
  - not only how frequently the supervisor will object to its aggressive risk taking ( $\int_0^t [(1 - \gamma) t + \gamma (1 - t)] dF(t)$ )
  - but also how costly those supervisory objections will be ( $c$ )
    - so increasing  $c$  can offset the control-dilution effect of increased  $\gamma$
- Our analysis taking  $c$  as given reflects the fact that the supervisor can be agile in his communication strategy, but he cannot freely adjust the bank's cost in case of supervisory objection.
  - Yet the supervisor does have the power to occasionally change such costs for the bank by passing legislation to promote financial stability.
    - e.g., the Dodd-Frank Act made all banks with assets above \$50 billion subject to a much more aggressive supervisory regime, effectively raising  $c$  for mid-sized banks;
    - in 2018, Congress scaled back Dodd-Frank, raising the threshold for increasing scrutiny of banks from \$50 billion to \$240 billion, effectively reducing  $c$  for mid-sized banks.

# Bank's Cost in Case of Supervisory Objection, Cont.

- To the extent that the supervisor has some control over the bank's cost, the proposition has an important policy implication.
  - It is optimal to err on the side of giving the supervisor too much power *in case he finds that the bank does not meet supervisory expectations.*
    - if  $c$  is too high, the supervisor could simply scale back how frequently he will object to aggressive risk-taking after having sent  $m = (1, 0)$
    - if  $c$  is too low, not only is the supervisor's unconstrained optimum infeasible (leaving welfare on the table), but the economy is exposed to experiencing a welfare loss in case the bank experiences a sudden boost in its private information



# Additional Commitment to the Supervisory Ruling

- Our baseline model does not give the supervisor commitment power over his follow-up supervisory ruling.
  - the supervisor allows aggressive risk-taking only when it is ex post efficient:
    - he will allow the bank's aggressive risk-taking if and only if he is of type  $t \geq \underline{t}$  ( $t \geq \hat{t}$ ) after having sent  $m = (1, 0)$  ( $m = (1, 1)$ )
- We now turn attention to the case where the supervisor also has commitment power over his follow-up supervisory ruling.
  - the supervisor can commit a priori to allowing (objecting to) aggressive risk-taking even if it is ex post inefficient
    - e.g., he will object to the bank's aggressive risk-taking if he is of type  $t \in T_{\text{Object}}^{(1,0)} \cap [\underline{t}, \bar{t})$  although he prefers ex post to allow it

# Additional Commitment to the Supervisory Ruling, Cont.

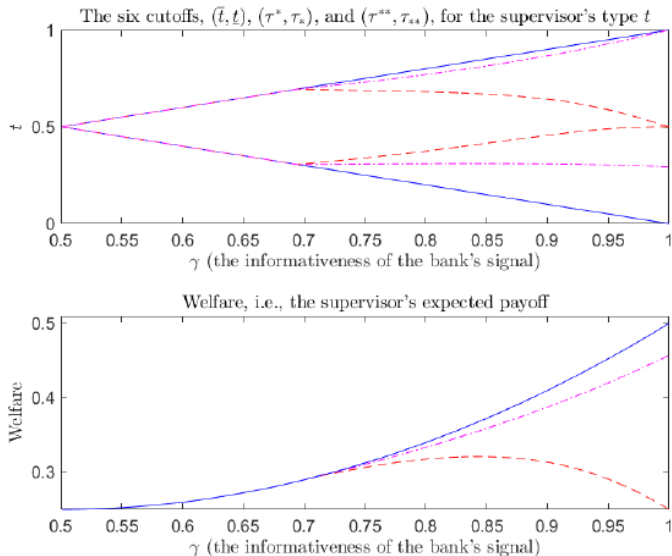
- As in the baseline model, it continues to hold that  $T_{\text{Allow}}^{(1,0)} = [\tau_{**}, \tau^{**})$  for some  $\tau_{**} \in (\underline{t}, \hat{t})$  and  $\tau^{**} \in (\hat{t}, \bar{t})$ .
- In contrast to our baseline model, it is straightforward to prove that  $\tau = \tau_{**} - T_{\text{Object}}^{(1,0)} = [0, \tau_{**})$  and  $T^{(1,0)} = [0, \tau^{**})$ .
  - in the baseline model,  $T_{\text{Object}}^{(1,0)} = [0, \underline{t})$  and  $T^{(0,0)} = [\underline{t}, \tau_*)$ .
  - intuitively, the supervisor of type  $t \in [\underline{t}, \tau_*)$  is tempted to respect the bank's decisions if they were reflective of its signal
    - sending  $m = (1, 0)$  in this region would make the IC constraint even more binding, so he resorted to sending  $m = (0, 0)$  instead
  - now, the supervisor is able to put this region to good use with the additional commitment power vested in him
    - he can overcome the temptation to respect the bank's risk-taking decision if  $t$  turns out to be in  $[\underline{t}, \tau_*)$  by committing to object to aggressive risk-taking in this region even after having sent  $m = (1, 0)$

## Proposition

*The supervisor's expected payoff with additional commitment is strictly monotone-increasing in  $\gamma$  on the interval  $(\frac{1}{2}, 1)$ .*

- The above proposition shows that, unlike in our baseline model, the supervisor can do strictly better than with cheap talk even as  $\gamma \rightarrow 1$ .
- The proposition shows that, with additional commitment to the supervisory ruling, more information does result in higher welfare.
  - The policy implication is that it is important to give the supervisor enough commitment power, particularly in the form of supervisory ruling.
    - Commitment power over how much he discloses about his own information alone can be impotent

# An Example



## An Example, Cont.

- As discussed above, the figure confirms that, unlike in the baseline model, the supervisor can do strictly better than with cheap talk even in the limit as  $\gamma \rightarrow 1$ .
- While it still is the case that the supervisor cannot attain his unconstrained optimum, the figure shows that the supervisor can do surprisingly well even in the limit as  $\gamma \rightarrow 1$ 
  - the welfare gap from the unconstrained optimum is visibly small
  - it is easy to check that, as shown in the figure,  $\tau^{**} \rightarrow 1$  in this limit
    - so the supervisor can induce the bank to reveal its information whenever he is optimistic enough
- Thus, it vividly reinforces the policy implication of the last proposition
  - it is important to give the supervisor enough commitment power, particularly in the form of supervisory ruling

# Conclusion

- The welfare effect of increased private information in the hands of the private sector is non-monotonic!
- The bank's cost in case of supervisory objection ought to be set high.
  - intuitively, what the bank cares about is the “cost-adjusted” probability that the supervisor will object to its aggressive risk-taking
  - some criticism around stress testing is that capping dividend and suspending share repurchases are too severe as disciplinary measures
  - however, it is not at discretion of the supervisor to reset this cost from one period to the next
  - we show that, if the cost of rejection is too low, it can hamstring the supervisor
  - we also show that, if the cost of rejection is too high, the supervisor can always achieve an unconstrained optimum by introducing strategic ambiguity into his communication strategy